

4.7

To bring the 1st charge in to construct the dipole requires
 an energy of:

$$-q \int_{\infty}^d \vec{E} \cdot d\vec{l} \quad \text{To bring the negative charge in requires}$$

$$-q \int_{\infty}^d \vec{E} \cdot d\vec{l} \quad \text{from the field and}$$

$$\frac{-q^2}{4\pi\epsilon_0 d} \quad \text{from the 1st charge.}$$

Putting this all together,

$$W = -q \int_0^d \vec{E} \cdot d\vec{l} - q \int_d^{\infty} \vec{E} \cdot d\vec{l} + q \int_d^{\infty} \vec{E} \cdot d\vec{l} = -\frac{kq^2}{d}$$

However, in the limit $d \rightarrow 0$, q must increase such that $\vec{p} = q\vec{d} = \text{constant}$.

This has the overall effect of causing $\frac{kq^2}{d}$ to vanish.

$$\text{Then } W = -q \int_0^d \vec{E} \cdot d\vec{l} = -q\vec{d} \cdot \vec{E} = -\vec{p} \cdot \vec{E}$$