

3.1

Inside the sphere  $z < R$ , so in the final line of the equation given above on page 118,  $z-R$  becomes  $R-z$ .

So then

$$V_{\text{ave}} = \frac{q_{\text{enc}}}{4\pi\epsilon_0} \frac{1}{2zR} [(z+R) - (R-z)] = \frac{2zq_{\text{enc}}}{4\pi\epsilon_0 2zR} = \frac{q_{\text{enc}}}{4\pi\epsilon_0 R}$$

In general, for an arbitrary number of spheres inside totaling, by the superposition principle  $V_{\text{ave}} = V_{\text{inside}} + V_{\text{outside}}$

$V_{\text{inside}} = \frac{q_{\text{enc}}}{4\pi\epsilon_0 R}$  as shown above. and  $V_{\text{outside}} = \frac{q}{4\pi\epsilon_0 R} = V_{\text{center}}$

as shown on pages 117-118. So,

$$V_{\text{ave}} = V_{\text{inside}} + \frac{q_{\text{enc}}}{4\pi\epsilon_0 R}$$

3.2

The charges will push each other away or attract each other until they are so close the weak force begins interacting.